

Received January 30, 2019, accepted February 27, 2019, date of publication March 5, 2019, date of current version March 25, 2019.

Digital Object Identifier 10.1109/ACCESS.2019.2903214

# Towards Energy-Efficient Underlaid Device-to-Device Communications: A Joint Resource Management Approach

RUI ZHANG<sup>1</sup>, (Member, IEEE), CHUHAN QI<sup>1</sup>, YONGZHAO LI<sup>1</sup>, (Senior Member, IEEE),  
YUHAN RUAN<sup>1</sup>, (Member, IEEE), CHENG-XIANG WANG<sup>2</sup>, (Fellow, IEEE),  
AND HAILIN ZHANG<sup>1</sup>, (Member, IEEE)

<sup>1</sup>State Key Laboratory of Integrated Services Networks, Xidian University, Xi'an 710071, China

<sup>2</sup>National Mobile Communications Research Laboratory, School of Information Sciences and Engineering, Southeast University, Nanjing 210096, China

Corresponding author: Yongzhao Li (yzhli@xidian.edu.cn)

This work was supported in part by the National Key R&D Program of China under Grant 2016YFB1200202, in part by the National Natural Science Foundation of China under Grant 61771365, in part by the Natural Science Foundation of Shaanxi Province under Grant 2017JZ022, in part by Fundamental Research Funds for the Central Universities, in part by the 111 Project under Grant B08038, in part by the Fundamental Research Funds for the Central Universities under Grant 2242019R30001, and in part by the EU H2020 RISE TESTBED project under Grant 734325.

**ABSTRACT** With increasing demands of green wireless communications, energy-efficient device-to-device (D2D) communications have attracted increasing attention. However, with resource sharing in an underlying manner, the system performance may be greatly degraded by the co-channel interference. For friendly coexistence of D2D and cellular communications, in this paper, we propose a joint resource management scheme where direct mode, two-hop mode, and cooperative mode are supported. Specifically, the joint resource management is formulated as a three-dimensional (3-D) *power-mode-channel* problem that maximizes the overall energy efficiency (EE) of D2D communications while guaranteeing the quality of service (QoS) of both D2D and cellular communications. To solve the formulated problem, the 3-D problem is decoupled by employing the orthogonality of different D2D links and the uniqueness of transmission mode for one D2D pair. Besides, considering that the introduction of cooperative mode increases the complexity of 3-D resource allocation algorithm, on the basis of the optimal scheme, we further propose a sub-optimal scheme to reduce the average time complexity. The simulation results verify the viability of the proposed schemes and reveal the impacts of system parameters such as the QoS, the distance between D2D source and destination, the location of the relay, and the number of D2D pairs on the EE of D2D systems.

**INDEX TERMS** Device-to-device communications, energy efficiency, power allocation, mode selection, channel assignment.

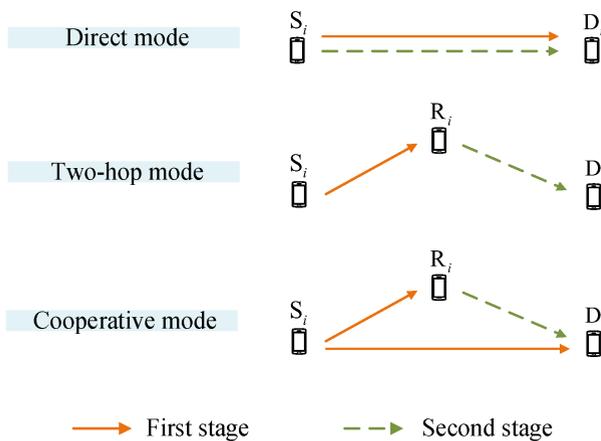
## I. INTRODUCTION

Without extra hops through base station (BS), Device-to-Device (D2D) communications underlying licensed cellular networks have great potentials to alleviate the extra construction and maintenance costs in the exponential explosion of smart devices and mobile applications [1], [2]. Besides, being able to reduce end-to-end delay, the D2D communication is also conceived as an alternative paradigm to support local area services [3], [4], intelligent transportation systems [5], and smart cities [6]. In particular, due to the nature of

proximity services, D2D communications can reduce the power consumption and increase the spectral efficiency (SE) significantly. As a result, the energy efficiency (EE) may be improved, supporting the low-carbon wireless communications in the incoming fifth generation (5G) networks [7].

Although the superiority of reusing cellular channels has been demonstrated in [8], the mutual interference caused by channel reusing is still a major obstacle in achieving EE promotion of D2D communications and guaranteeing the performance of the existing cellular users [9], [10]. Therefore, effective interference management schemes are eager to be employed to mitigate the negative impacts of the mutual interference. Power allocation and channel assignment are

The associate editor coordinating the review of this manuscript and approving it for publication was Mauro Fadda.



**FIGURE 1.** The three transmission modes of D2D communications.

two effective approaches to mitigate the interference and therefore can improve the EE. In addition, the transmission mode of D2D pairs also has a significant impact on the performance of the system. As shown in Figure 1, three typical modes, namely, direct-mode, two-hop mode, and cooperative mode, are illustrated. In two-hop mode, the D2D receiver only receive signals from relay user in second phase. In cooperative mode, D2D receiver receive signals from D2D transmitter in the first phase and signals from relay users in second phase, and conduct combination of signals of different phases. With the assistance of the relay, the D2D communication in two-hop mode [11], [12] or cooperative mode experiences smaller pathloss attenuation and then the received signal is stronger. Thus, they outperform the D2D communication in direct mode in terms of SE and are widely utilized in emergency communications and social-aware local area networks [13], [14]. But the circuit power, which is included in the total power consumed, increases with the additional reception/transmission of the relay and destination [15]. Therefore cooperative mode or two-hop mode may not be superior to direct mode in terms of EE. From the above understanding, it is desired to investigate a 3-D *power-mode-channel* resource management approach for D2D communications to optimize EE, which is a critical performance metric for 5G networks but has not been well studied in D2D communications with different transmission modes in Figure 1.

## II. BACKGROUND AND CONTRIBUTIONS

In the regard of resource management, various schemes and algorithms have been proposed to improve the performance of D2D communications underlying cellular networks. For power allocation, Lee *et al.* [16], Liu *et al.* [17] studied the problem when the D2D communication is in direct mode. In [16], the proposed centralized algorithm calculated the optimal power values of D2D pairs to maximize the signal-to-interference-plus-noise ratio (SINR) of the cellular user, while the proposed distributed algorithm maximize the SE of D2D users. In [17], the geometric programming technique

was adopted to optimize the sum rate of the cellular user and the D2D user when giving priority to cellular communications. In order to get power values of the source and relay simultaneously, an effective iterative method was proposed by applying the nonlinear fractional programming when considering the SE of cellular users in [18]. In addition, for channel assignment in [19] and [20] optimizing the sum rate, Hussain *et al.* [19] focused the scenario where one D2D pair shared multiple cellular channels, as well as multiple D2D pairs shared a single cellular channel. The solution for D2D communications underlying full duplex cellular networks was proposed in [20].

These aforementioned studies conducted resource management from the perspective of power allocation or channel assignment separately. To further improve the system performance, two-dimensional (2-D) resource management schemes were adopted in [21]–[29]. The power allocation and channel assignment were discussed in [21]–[25] to maximize EE. Xu *et al.* [21], Jiang *et al.* [22], and Zhou *et al.* [23] decoupled the problem and proposed iteration algorithms. A iteration algorithm with low complexity was proposed in [21]. In [22], the optimal power values on all candidate channels were obtained firstly and then channel assignment finished. A many-to-one matching algorithm was proposed to solve the problem with varying preferences in [23]. Besides, Zhou *et al.* [24], [25] considered a multi-objective optimization problem, maximizing the EE of D2D users and maximizing the EE of cellular users, and the intracell interference respectively. Furthermore, the authors discussed 2-D *power-mode* algorithms in [26]–[28] and 2-D *mode-channel* algorithms in [29]. From the perspective of candidate working modes, cellular mode and overlay mode were discussed in [26], while overlay mode and underlay mode were considered in [27]. More specifically, Ma *et al.* [28] compared cellular mode, overlay mode, and underlay mode to achieve the minimum power consumption. Considering the three working modes, the algorithm in [29] was proposed to increase the sum rate.

Although the resource management algorithms have been widely studied, these papers concentrating on the one-dimensional (1-D) or the 2-D resource management cannot fully exploited the possible enhancement of system performance [30]. For D2D communications with relays, Guo *et al.* [31], Hoang *et al.* [32], Ma *et al.* [33] only focused on direct mode and two-hop mode. The cooperative mode, which brings higher SE but consumes more power, has not been carefully measured. Thus, cooperative mode should be deliberated with direct mode and two-hop mode to increase EE.

Until now, 3-D resource allocation schemes for D2D communication with direct mode, two-hop mode, and cooperative mode have not been investigated. For such a D2D communication scenario with various transmission modes and multiple dimensions of resource, it is imperative to investigate a general resource allocation scheme to achieve EE enhancement and friendly coexistence of D2D and

cellular communications. Moreover, since the introduction of cooperative mode increases the complexity of 3-D resource allocation, it is challenging to design a low-complexity 3-D resource allocation algorithm. The main contributions of our work are summarized as follows:

- To realize energy efficient D2D communications, a joint power allocation, mode selection, and channel assignment scheme for underlaid D2D communications is proposed in this paper, where three transmission modes,<sup>1</sup> i.e., direct mode, two-hop mode, and cooperative mode, are all taken into account. In particular, for friendly coexistence of D2D and cellular communications, the 3-D resource allocation problem is formulated to maximize EE of D2D communications while guaranteeing the quality of service (QoS) of both D2D and cellular communications.
- We design a specific procedure for the complicated 3-D resource allocation problem, where transmit power, reusing channel, and transmission mode are coupled to each other. Employing the orthogonality of different D2D links and the uniqueness of transmission mode for one D2D pair, we firstly decouple the original 3-D problem. Then, an alternating Dinkelbach algorithm is proposed to obtain the optimal transmit power of D2D communications in different transmission mode.
- Considering that the cooperative mode increase EE of D2D communications at the expense of high complexity of algorithm, a low-complexity sub-optimal 3-D resource allocation algorithm is proposed for the sake of practical implementation. Referring to the fact that the transmission mode that can obtain largest EE of one D2D pair does not obviously vary from one channel to another, thus, we utilize the mode selection result on random channel as the final result, reducing the complexity of 3-D resource allocation algorithm. Also, theoretical analysis of time complexity is presented to demonstrate the reduction.

A summary of notations and key parameters in this paper is given in Table 1.

The remainder of this paper is organized as follows. Section III introduces the system model. In Section IV, we present the problem formulation, simplify the objective function, and give the optimal scheme. Section V shows the low-complexity sub-optimal scheme and the time complexity analysis. In Section VI, the performance of our proposed algorithms is illustrated by the simulation results. Finally, conclusions are drawn in Section VII.

### III. SYSTEM MODEL

We consider a single cell scenario with  $M$  cellular user equipments (CUEs) (i.e.,  $\mathcal{C} = \{C_j\}$ ) communicating with BS on

<sup>1</sup>We do not discuss cellular mode and overlay mode. On one hand, the simulations in [34] illustrated that the percentage of cellular mode being selected as the optimal mode under EE-based scheme is the lowest compared with overlay mode and underlay mode. On the other hand, the co-channel interference is not considered in overlay mode. The solution in this paper can be extended to the overlay situation.

TABLE 1. A summary of the notations and key parameters.

Notation	Description
$\mathcal{C}$	Set of cellular users
$\bar{\gamma}$	Average received SNR
$\mathcal{CN}(\cdot)$	Complex additive white Gaussian distribution
$1/\lambda$	Drain efficiency of power amplifier
$\eta$	EE of D2D pairs
$\mu_{ij}$	Coefficient of channel assignment
$\omega_{ij}^k$	Coefficient of mode selection
$\Upsilon_{th}^D, \Upsilon_{th}^C$	Rate threshold of D2D pairs, and cellular users
$\Pi$	EE Matrix
$\Omega, \Phi, \Theta$	Feasible region of variables
$\varepsilon$	Permissible error in Algorithm 1
$\mathcal{O}(\cdot)$	Time complexity

Parameter	Description
$M, N$	Number of cellular users, and number of D2D pairs
$C_j$	$j$ -th cellular user
$S_i, R_i, D_i$	Source user, relay user and destination user of the $i$ -th D2D pair
$h_{XY}$	Channel coefficient of $X \rightarrow Y$ link
$P_X$	Transmit power of user X
$P_{cps}^k$	Circuit power in the $k$ -th mode
$R_X^k$	SE of user X in the $k$ -th mode

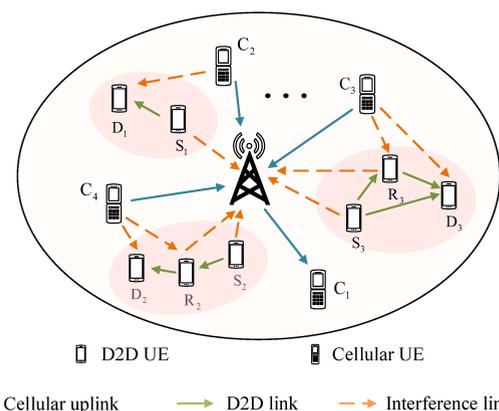


FIGURE 2. A single-cell scenario with D2D communications underlaying the cellular network.

orthogonal channels and  $N$  ( $M \geq N$ ) D2D pairs, as shown in Figure 2. No idle orthogonal cellular channel can be used by D2D pairs, and they will reuse the channels when CUEs upload to BS. Notice that each D2D pair can only reuse one cellular channel, and each cellular channel is reused by only one D2D pair. The D2D pair consists of a source user equipment (i.e.,  $S_i$ ) and a paired destination user equipment (i.e.,  $D_i$ ). Besides, there are many idle user equipments (UEs) serve as candidate relays for D2D pairs to realize two-hop or cooperation communication. Our paper focuses on the

scene that relay selection has been accomplished considering remaining battery time, pathloss and social relationship. The D2D pair may have one appropriate relay (i.e.,  $R_i$ ) or not.

Network resource usage information and channel state information (CSI) between users and BS are also essential for resource management for original cellular networks without D2D communications. Only CSI between D2D users is the extra information needed, which can be obtained through neighbor discovery [35], [36]. Thus, BS can have CSI of all links. It is assumed that each UE is equipped with a single antenna. Meanwhile, BS controls the transmit power of CUEs such that the uplink signals are received with the same signal-to-noise ratio (SNR), and allocates power, selects mode, assigns channel for D2D pairs. In this paper, let  $h_{XY}$  denote the channel coefficient of  $X \rightarrow Y$  link. Specifically,  $h_{s_i d_i}$ ,  $h_{s_i r_i}$ ,  $h_{r_i d_i}$ , and  $h_{c_j e}$  are the channel coefficients of  $S_i \rightarrow D_i$ ,  $S_i \rightarrow R_i$ ,  $R_i \rightarrow D_i$ , and  $C_j \rightarrow BS$  communication links, respectively.  $h_{c_j r_i}$ ,  $h_{c_j d_i}$ ,  $h_{r_i e}$ , and  $h_{s_i e}$  are the channel coefficients of  $C_j \rightarrow R_i$ ,  $C_j \rightarrow D_i$ ,  $R_i \rightarrow BS$ , and  $S_i \rightarrow BS$  interfering links, respectively. We model the channel coefficient as  $h_{XY} = g_{XY}^{pl} \cdot g'_{XY}$ , where  $g_{XY}^{pl}$  denotes the pathloss, and  $g'_{XY}$  denotes the fast fading coefficient. The Nakagami- $m$  channel model, which can simulate different signal fading environments, is employed to characterize above channels.<sup>2</sup> In this case, the probability density function (PDF) of  $|g'_{XY}|^2$  is expressed as follows:

$$f_{|g'_{XY}|^2}(\gamma) = \frac{\gamma^{m-1}}{\Gamma(m)} \left(\frac{m}{\bar{\gamma}}\right)^m e^{-\frac{m}{\bar{\gamma}}\gamma}, \quad \bar{\gamma} \geq 0, m \geq \frac{1}{2} \quad (1)$$

where  $m$  denotes the fading parameter and  $\bar{\gamma}$  denotes the average SNR [38]. The fading environment can be described from serious, moderate, slight to no fading by adjusting  $m$ . Specifically, we denote  $m_1$  for the communication links and  $m_2$  for the interference links.

### A. DIRECT MODE

Now we give a detail description of the three transmission modes, and derive the SE and the power consumption respectively. As shown in Figure 2, When  $i$ -th D2D pair is in direct mode reusing the channel of  $C_j$ ,  $S_i$  sends its data to  $D_i$  and  $C_j$  uploads to BS. During the transmission,  $S_i$  causes interference to BS, while  $D_i$  receives interference from  $C_j$ . The signals received at  $D_i$  and BS, which are denoted by  $z_{dij}$  and  $y_{c_{ij}}$ , respectively, can be expressed by

$$z_{dij} = \sqrt{P_{s_{ij}}} h_{s_i d_i} x_s + \sqrt{P_{c_j}} h_{c_j d_i} x_c + n_1 \quad (2)$$

$$y_{c_{ij}} = \sqrt{P_{c_j}} h_{c_j e} x_c + \sqrt{P_{s_{ij}}} h_{s_i e} x_s + n_2 \quad (3)$$

where  $P_{s_{ij}}$  and  $P_{c_j}$  denote the transmit power of  $S_i$  and  $C_j$ , respectively,  $x_s$  and  $x_c$  denote the signals transmitted from  $S_i$  and  $C_j$ , respectively,  $n_1$  and  $n_2$  denote the noises. In this paper, all the noises are complex additive white Gaussian noises (AWGNs) with distribution  $\mathcal{CN}(0, N_0)$ .

<sup>2</sup> Our work focuses on the resource management problem, thus the Nakagami- $m$  channel model is employed. In the future, we will consider a more general channel model, such as [37].

Accordingly, the SE of the  $i$ -th D2D link and the  $j$ -th cellular link, denoted by  $R_{dij}^1$  and  $R_{c_{ij}}^1$ , respectively, are expressed by

$$R_{dij}^1 = \log_2 \left( 1 + \alpha_{ij} P_{s_{ij}} \right) \quad (4)$$

$$R_{c_{ij}}^1 = \log_2 \left( 1 + \frac{P_{c_j} |h_{c_j e}|^2}{P_{s_{ij}} |h_{s_i e}|^2 + N_0} \right) \quad (5)$$

where  $\alpha_{ij} = \frac{|h_{s_i d_i}|^2}{P_{c_j} |h_{c_j d_i}|^2 + N_0}$ . Then, the power consumption in direct mode  $P_{dij}^1$  is

$$P_{dij}^1 = \lambda P_{s_{ij}} + P_{c_{ps}}^1 \quad (6)$$

where  $P_{c_{ps}}^1 = P_{ss} + P_{dd}$ ,  $\lambda P_{s_{ij}}$  is the radio-frequency power of  $S_i$ , with  $1/\lambda \in (0, 1]$  denoting the drain efficiency of power amplifier. Besides,  $P_{ss}$  denotes the circuit power of transmitting data at  $S_i$ ,  $P_{dd}$  denotes the circuit power of receiving data at  $D_i$ .

### B. TWO-HOP MODE

If the D2D pair has an appropriate relay, two-hop mode and cooperative mode are available. As shown in Figure 2, when  $i$ -th D2D pair is in two-hop mode reusing the channel of  $C_j$ , one complete transmission finishes in two phases. In the first phase,  $S_i$  sends its data to  $R_i$ . At the same time,  $S_i$  causes interference to BS, and  $R_i$  receives interference from  $C_j$ . The signals received at  $R_i$  and BS, denoted by  $x_r$ , and  $y_{c_{1ij}}$ , respectively, can be expressed by

$$x_r = \sqrt{P_{s_{ij}}} h_{s_i r_i} x_s + \sqrt{P_{c_j}} h_{c_j r_i} x_c + n_3 \quad (7)$$

$$y_{c_{1ij}} = \sqrt{P_{c_j}} h_{c_j e} x_c + \sqrt{P_{s_{ij}}} h_{s_i e} x_s + n_4. \quad (8)$$

In the second phase,  $R_i$  amplifies and forwards the received signal in the first stage to  $D_i$ . At the same time,  $R_i$  causes interference to BS, and  $D_i$  receives interference from  $C_j$ . According to [39], the amplifier gain of  $R_i$  can be expressed by  $G_{ij} = 1 / \sqrt{P_{s_{ij}} |h_{s_i r_i}|^2 + P_{c_j} |h_{c_j r_i}|^2 + N_0}$ . The signals received at  $D_i$  and BS, denoted by  $z_{dij}$  and  $y_{c_{2ij}}$ , respectively, can be expressed by

$$z_{dij} = \sqrt{P_{r_{ij}}} h_{r_i d_i} G_{ij} x_r + \sqrt{P_{c_j}} h_{c_j d_i} x_c + n_5 \quad (9)$$

$$y_{c_{2ij}} = \sqrt{P_{c_j}} h_{c_j e} x_c + \sqrt{P_{r_{ij}}} h_{r_i e} x_r + n_6 \quad (10)$$

where  $P_{r_{ij}}$  denotes the transmit power of  $R_i$ .

From (7) - (10), the SE of the  $i$ -th D2D link and the  $j$ -th cellular link, denoted by  $R_{dij}^2$  and  $R_{c_{ij}}^2$ , respectively, are expressed by

$$R_{dij}^2 = \frac{1}{2} \log_2 \left( 1 + \frac{\beta_{ij} \gamma_{ij} \cdot P_{s_{ij}} P_{r_{ij}}}{1 + \gamma_{ij} P_{r_{ij}} + \beta_{ij} P_{s_{ij}}} \right) \quad (11)$$

$$R_{c_{ij}}^2 = \frac{1}{2} (\log_2 (\kappa_{ij} P_{c_j}) + \log_2 (\rho_{ij} P_{c_j})) \quad (12)$$

where  $\beta_{ij} = \frac{|h_{s_i r_i}|^2}{P_{c_j} |h_{c_j r_i}|^2 + N_0}$ ,  $\gamma_{ij} = \frac{|h_{r_i d_i}|^2}{P_{c_j} |h_{c_j d_i}|^2 + N_0}$ ,  $\kappa_{ij} = \frac{|h_{c_j e}|^2}{P_{s_{ij}} |h_{s_j c_j}|^2 + N_0}$ ,  $\rho_{ij} = \frac{|h_{c_j e}|^2}{P_{r_{ij}} |h_{r_i c_j}|^2 + N_0}$ . Note that the coefficient  $1/2$  accounts for the fact that the two-hop D2D occurs during two phases. Then, the power consumption in two-hop mode  $P_{dij}^2$  is

$$P_{dij}^2 = \frac{1}{2} (\lambda P_{s_{ij}} + \lambda P_{r_{ij}} + P_{cps}^2) \quad (13)$$

where  $P_{cps}^2 = P_{ss} + P_{dd} + 2P_{rr}$ ,  $\lambda P_{r_{ij}}$  is the radio-frequency power of  $R_i$ , and  $P_{rr}$  denotes the circuit power of reception and transmission at  $R_i$ .

### C. COOPERATIVE MODE

As shown in Figure 2, when  $i$ -th D2D pair is in cooperative mode reusing the channel of  $C_j$ ,  $D_i$  receives the data from  $S_i$  and  $R_i$ , and then combines the signals using the maximal ratio combining (MRC) to achieve the cooperation diversity. The complete transmission consists of two time phases. In the first phase,  $S_i$  broadcasts signal while  $R_i$  and  $D_i$  listen.  $R_i$  and  $D_i$  receive interference from  $C_j$ . The signals received at  $R_i$  and BS are similar to (7) and (8), respectively, while the signal received at  $D_i$ , denoted by  $z_{d1ij}$ , can be expressed by

$$z_{d1ij} = \sqrt{P_{s_{ij}}} h_{s_i d_i} x_s + \sqrt{P_{c_j}} h_{c_j d_i} x_c + n_7. \quad (14)$$

The second phase is similar to that in two-hop mode. The signals received at  $D_i$  and BS are similar to (9) and (10), respectively.

Similar to direct mode and two-hop mode, the SE of the  $i$ -th D2D link and the  $j$ -th cellular link, denoted by  $R_{dij}^3$  and  $R_{c_{ij}}^3$ , respectively, are expressed by

$$R_{dij}^3 = \frac{1}{2} \log_2 \left( 1 + \alpha_{ij} P_{s_{ij}} + \frac{\beta_{ij} \gamma_{ij} \cdot P_{s_{ij}} P_{r_{ij}}}{1 + \gamma_{ij} P_{r_{ij}} + \beta_{ij} P_{s_{ij}}} \right) \quad (15)$$

$$R_{c_{ij}}^3 = \frac{1}{2} (\log_2 (\kappa_{ij} P_{c_j}) + \log_2 (\rho_{ij} P_{c_j})). \quad (16)$$

Then, the power consumption in cooperative mode  $P_{dij}^3$  is

$$P_{dij}^3 = \frac{1}{2} (\lambda P_{s_{ij}} + \lambda P_{r_{ij}} + P_{cps}^3) \quad (17)$$

where  $P_{cps}^3 = P_{ss} + 2P_{dd} + 2P_{rr}$ .

## IV. JOINT RESOURCE MANAGEMENT FOR ENERGY-EFFICIENT D2D COMMUNICATIONS

In this section, we formulate the 3-D *power-mode-channel* optimization problem of our system model. By employing the orthogonality in different D2D links and the uniqueness of transmission mode, the problem is decoupled without loss of optimality. The specific steps of the optimal scheme will be presented at last.

### A. PROBLEM FORMULATION

To better adapt to the requirements of green wireless communications in 5G, especially the low power consumption and high throughput, we intend to improve the overall EE of D2D communications. Meanwhile, from a practical perspective, both D2D and cellular users expect high data rate to support various services and applications like Internet access and data downloading. Thus, the a 3-D *power-mode-channel* resource management approach is formulated to maximize the EE of D2D communications while guaranteeing the QoS of both D2D and cellular users. According to [40], the EE of the  $i$ -th D2D pair reusing the  $j$ -th channel, denoted by  $\eta_{ij}$ , can be expressed by

$$\eta_{ij} = \frac{R_{ij}}{P_{ij}} \quad (18)$$

where

$$R_{ij} = \sum_{k=1}^3 \omega_{ij}^k R_{dij}^k \quad (19)$$

$$P_{ij} = \sum_{k=1}^3 \omega_{ij}^k P_{dij}^k \quad (20)$$

where  $\omega_{ij}^k = 1$  denotes that the corresponding mode  $k$  is selected and otherwise  $\omega_{ij}^k = 0$ . If the D2D pair has no relay, the direct mode will be selected, which means  $\omega_{ij}^1 = 1$ .

In summary, by denoting the system EE as  $\eta$ , the optimization problem can be formulated as

$$\text{maximize } \eta = \sum_{i=1}^N \sum_{j=1}^M \mu_{ij} \eta_{ij} \quad (21)$$

$$\text{subject to } \sum_{i=1}^N \mu_{ij} \leq 1 \quad (22)$$

$$\sum_{j=1}^M \mu_{ij} = 1 \quad (23)$$

$$\mu_{ij} \in \{0, 1\} \quad (24)$$

$$\sum_{k=1}^3 \omega_{ij}^k = 1, \omega_{ij}^k \in \{0, 1\} \quad (25)$$

$$R_{dij}^k \geq \Upsilon_{th}^D, R_{c_{ij}}^k \geq \Upsilon_{th}^C \quad (26)$$

$$P_{s_{ij}} \leq P_{max}, P_{r_{ij}} \leq P_{max} \quad (27)$$

where  $\mu_{ij} = 1$  denotes that the  $i$ -th D2D pair reuses the  $j$ -th channel and otherwise  $\mu_{ij} = 0$ . Constraint (22) guarantees that each cellular channel is reused by only one D2D pair, but not all channels will be reused. Constraint (23) guarantees each D2D pair reuses only one cellular channel. Constraints (22)-(24) ensure the orthogonality of different D2D links. Constraint (25) guarantees the uniqueness of transmission mode for one D2D pair. Constraints (26) assures the minimum required rate  $\Upsilon_{th}^D$  of D2D links and  $\Upsilon_{th}^C$  of cellular links. Constraint (27) restricts maximal transmit power of  $S_i$  and  $R_i$  by  $P_{max}$ .

In this problem, the transmit power, the transmission mode and the reusing channel are unknown. Clearly, the assignment of channels impacts the channel gains between the D2D pairs and CUEs, and hence influences the optimal power values. Furthermore, the optimal power values depend on the transmission mode of D2D pairs. Therefore, there is a mutual dependence among three variables. More complicated, the function is nonlinear fractional and non-concave. As we know, Exhaustive Attack method is effective but with high complexity even for a small-size system. Therefore, we concentrate on an efficient solution.

**B. AN OPTIMAL SOLUTION TO THE 3-D RESOURCE PROBLEM**

According to [22] and [41], constraints (23) and (24) guarantee that for the  $i$ -th D2D pair,  $\exists j' \in j, \mu_{ij'} = 1$ , then  $\mu_{ij} = 0$  ( $j \neq j'$ ). The optimal solution of the original problem is also the optimal solution of the following equivalent optimization problem:

$$\begin{aligned} & \text{maximize} && \eta = \sum_{i=1}^N \mu_{ij} \eta_{ij} \\ & \{P_{ij}, \omega_{ij}^k, \mu_{ij}\} \\ & \text{subject to} && (22) - (27). \end{aligned} \tag{28}$$

Constraint (22) and (24) guarantee that for the  $j$ -th channel,  $\forall i' \in i$ , if  $\mu_{i'j} = 1$ , then  $\mu_{ij} = 0$  ( $i \neq i'$ ), which means the channels reused by two D2D pairs are different and hence there is no co-channel interference between D2D pairs. Therefore, the problem in (28) can be further expressed as the following equivalent independent optimization problems:

$$\begin{aligned} & \text{maximize} && \eta_{ij} \\ & \{P_{ij}, \omega_{ij}^k\} \\ & \text{subject to} && (25) - (27) \end{aligned} \tag{29}$$

$$\begin{aligned} & \text{maximize} && \eta = \sum_{i=1}^N \mu_{ij} \eta_{ij} \\ & \{\mu_{ij}\} \\ & \text{subject to} && (22) - (24). \end{aligned} \tag{30}$$

Problem (29) means to get the optimal EE for D2D pairs in all candidate channels. To solve (29), we need to compare the EE values of three modes and decide which mode is suitable for the  $i$ -th D2D pair on the  $j$ -th channel considering the uniqueness of transmission mode. Obviously, direct mode is selected for the D2D pairs without relays. Moreover, problem (30) can be regarded as a maximum match problem of a bipartite graph, which can be solved by Hungarian algorithm. As in Figure 3,  $\eta_{ij}$  can be regarded as the weight of two vertex sets, cellular channels and D2D pairs in our problem. If the  $i$ -th D2D pair cannot reuse the  $j$ -th channel because of serious interference, we set  $\eta_{ij}$  as  $+\infty$ .

In the light of our analysis, the number of candidate modes depends on the existence of the relay, it is necessary to divide D2D pairs into two groups. Therefore, the procedure of our solution to the original joint power allocation, mode selection and channel assignment optimization problem is composed of the following steps:

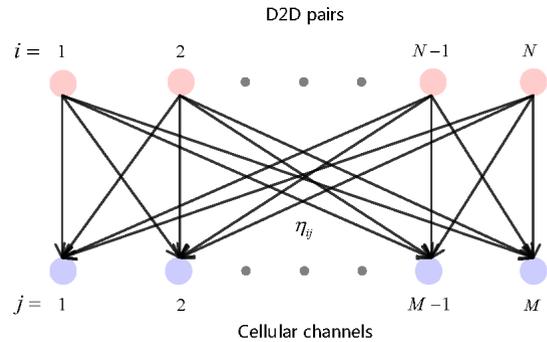


FIGURE 3. Bipartite graph of problem (30).

- 1) Group D2D pairs according to whether the relay exists.
- 2) For each D2D pair without relays in all candidate cellular channels, obtain the optimal power and EE values in direct mode, and select the EE as  $\eta_{ij}$ . For each D2D pair with relays in all candidate cellular channels, obtain the optimal power and EE values of three transmission modes, compare the EE values and select the largest one as  $\eta_{ij}$ .
- 3) For  $N$  D2D pairs and  $M$  cellular links, we have an EE matrix  $\Pi$ , which can be expressed as

$$\Pi = [\eta_{ij}]_{N \times M}. \tag{31}$$

- 4) Employ Hungarian algorithm to find the maximum match.
- 5) Determine the transmit power and mode according to the channel results.

From previous discussions, it can be seen that power allocation is the foundation of the whole solution. Thus, in the following, we firstly analyze power allocation in different modes separately and then, we propose a general algorithm to obtain optimal transmit power for D2D communications in different modes.

In direct mode, which means  $\omega_{ij}^1 = 1$ , the problem (29) can be expressed as

$$\begin{aligned} & \text{maximize} && \eta_{ij} = \frac{\log_2(1 + \alpha_{ij} P_{s_{ij}})}{\lambda P_{s_{ij}} + P_{cps}^1} \\ & \{P_{s_{ij}}\} \\ & \text{subject to} && (26) \text{ and } (27). \end{aligned} \tag{32}$$

The objective function in (32) is nonlinear and non-concave, thus we cannot apply standard convex optimization techniques to solve the fractional programming (FP) problem. For the optimal power value, Theorem 1 is introduced according to [42]. By denoting  $\Omega$  and  $\eta_{ij}^*$  as the feasible region and the maximal EE respectively, we have Theorem 1,

*Theorem 1:*  $\eta_{ij}^*$  is available if and only if

$$\text{maximize}_{\{P_{s_{ij}}\} \in \Omega} \left\{ R_{d_{ij}}^1 - \eta_{ij}^* (\lambda P_{s_{ij}} + P_{cps}^1) \right\} = 0. \tag{33}$$

*Proof:* The proof is similar to [43].

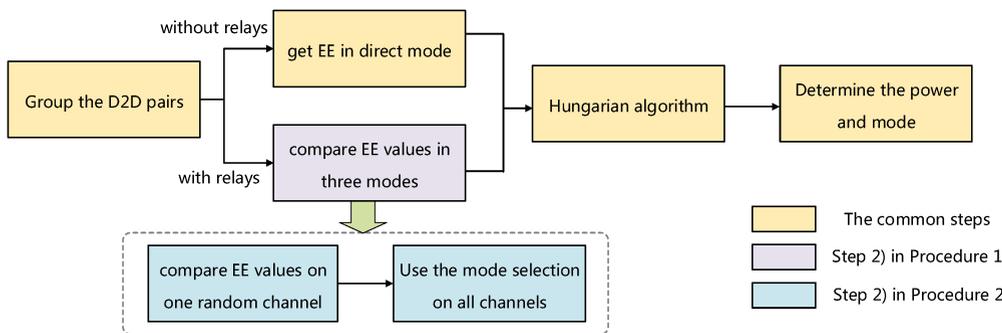


FIGURE 4. The illustration of Procedure 1 and Procedure 2.

It can be seen from Theorem 1 that an equivalent objective function in subtractive form exists for the considered objective function of (32) by exploiting the fractional programming form. According to [42], we can apply the Dinkelbach algorithm to solve it because the function is concave in  $P_{s_{ij}}$ . Although the Dinkelbach algorithm is widely utilized, we also present the details of this algorithm in Appendix to intuitively illustrate the power solution derivation.

In two-hop mode, we have  $\omega_{ij}^2 = 1$ . The problem (29) can be expressed as

$$\begin{aligned} & \underset{\{P_{s_{ij}}, P_{r_{ij}}\}}{\text{maximize}} \quad \eta_{ij} = \frac{\frac{1}{2} \log_2 \left( 1 + \frac{\beta_{ij} \gamma_{ij} P_{s_{ij}} P_{r_{ij}}}{1 + \gamma_{ij} P_{r_{ij}} + \beta_{ij} P_{s_{ij}}} \right)}{\frac{1}{2} (\lambda P_{s_{ij}} + \lambda P_{r_{ij}} + P_{\text{cps}}^2)} \\ & \text{subject to} \quad (26) \text{ and } (27). \end{aligned} \quad (34)$$

According to Theorem 1,  $\eta_{ij}^*$  is available if and only if

$$\underset{\{P_{s_{ij}}, P_{r_{ij}}\} \in \Phi}{\text{maximize}} \left\{ R_{d_{ij}}^2 - \frac{1}{2} \eta_{ij}^* (\lambda P_{s_{ij}} + \lambda P_{r_{ij}} + P_{\text{cps}}^2) \right\} = 0 \quad (35)$$

where  $\Phi$  denotes the feasible region in (34).

Similarly, in cooperative mode, the problem (29) can be expressed as

$$\begin{aligned} & \underset{\{P_{s_{ij}}, P_{r_{ij}}\}}{\text{maximize}} \quad \eta_{ij} = \frac{\frac{1}{2} \log_2 \left( 1 + \alpha_{ij} P_{s_{ij}} + \frac{\beta_{ij} \gamma_{ij} P_{s_{ij}} P_{r_{ij}}}{1 + \gamma_{ij} P_{r_{ij}} + \beta_{ij} P_{s_{ij}}} \right)}{\frac{1}{2} (\lambda P_{s_{ij}} + \lambda P_{r_{ij}} + P_{\text{cps}}^3)} \\ & \text{subject to} \quad (26) \text{ and } (27). \end{aligned} \quad (36)$$

According to Theorem 1,  $\eta_{ij}^*$  is available if and only if

$$\underset{\{P_{s_{ij}}, P_{r_{ij}}\} \in \Theta}{\text{maximize}} \left\{ R_{d_{ij}}^3 - \frac{1}{2} \eta_{ij}^* (\lambda P_{s_{ij}} + \lambda P_{r_{ij}} + P_{\text{cps}}^3) \right\} = 0 \quad (37)$$

where  $\Theta$  denotes the feasible region in (36).

Compared with (33), the objective functions in (35) and (37) are non-concave in  $P_{r_{ij}}$  and  $P_{s_{ij}}$ . However, they are concave in  $P_{s_{ij}}$  for a fixed  $P_{r_{ij}}$  and concave in  $P_{r_{ij}}$  for a fixed  $P_{s_{ij}}$ . Thus, we can utilize Dinkelbach algorithm to obtain optimal  $P_{s_{ij}}/P_{r_{ij}}$  for a fixed  $P_{r_{ij}}/P_{s_{ij}}$ . According to the alternating maximization (AM) algorithm in [44], we propose an alternating Dinkelbach algorithm to obtain the optimal

### Algorithm 1 Alternating Dinkelbach algorithm

**1: Initialization:**

$P_s^{(0)}, P_r^{(0)}, l = 0$ , permissible error  $\varepsilon = 10^{-3}$ .

2:  $P_s^{*(0)} = P_s^{(0)}, P_r^{*(0)} = P_r^{(0)}$ , calculate  $\eta^{(0)}$ .

**3: Iteration begins:**

4: Optimize over  $P_s^{*(l+1)}$  for a given  $P_r^{*(l)}$  by Dinkelbach algorithm.

5: Optimize over  $P_r^{*(l+1)}$  for a given  $P_s^{*(l+1)}$  by Dinkelbach algorithm.

6: Update the index  $l = l + 1$ .

7: Calculate  $\eta^{(l)}$ , if  $|\eta^{(l)} - \eta^{(l-1)}| > \varepsilon$ , return 4, otherwise continue.

**8: Iteration ends.**

9: Output  $P_s^{*(l)}, P_r^{*(l)}, \eta^* = \eta^{(l)}$ .

transmission power for D2D communications in two-hop and cooperative modes. As illustrated in Algorithm 1, the alternating Dinkelbach algorithm is an extension of Dinkelbach algorithm. For simplicity, we ignore  $i$  and  $j$ . Permissible error  $\varepsilon$  represents the maximum error between the output and the optimal point in fact.

As a conclusion, the aforementioned power allocation algorithms are employed for D2D pairs on all candidate channels. We compare the results and regard the largest EE value as the weight for each possible match. Then Hungarian algorithm is used and we can obtain the transmit power, transmission mode and reusing channel for each D2D pair. As illustrated in Figure 4, the specific procedure for the 3-D resource allocation are summarized as Procedure 1.

### V. A LOW-COMPLEXITY SOLUTION TO THE 3-D PROBLEM

To this end, we can employ Procedure 1 to conduct 3-D resource allocation for underlaid D2D communications including direct mode, two-hop mode, and cooperative mode. However, the introduction of cooperative mode increases the complexity of 3-D resource allocation algorithm. Thus, it is imperative to design a low-complexity 3-D resource allocation algorithm to facilitate practical application.

As can be seen from Figure 4, Procedure 1 is composed of three algorithms, Dinkelbach algorithm, AM algorithm and Hungarian algorithm. Firstly, it is shown that for non-linear fractional programming problems, Dinkelbach algorithm converges superlinearly in [45]. However, we can not quantitatively analyze the time complexity while it is related to the initial values and the permissible error. Thus we denote  $W_1$  and  $W_2$  as the iteration times for Dinkelbach algorithm and the outer iteration in AM algorithm, respectively. The time complexity for AM algorithm is  $\mathcal{O}(W_1 W_2)$ . Besides, we have  $N$  D2D pairs and  $M$  ( $M \geq N$ ) cellular channels in this paper. The time complexity for Hungarian algorithm is  $\mathcal{O}(M^3)$ . If we assume that all D2D pairs are equipped with relays, the average time complexity of Procedure 1 is  $\mathcal{O}(2M^2 W_1 W_2 + M^3)$ . When the cooperative mode is not involved, the average time complexity of Procedure 1 is  $\mathcal{O}(M^2 W_1 W_2 + M^3)$ . From the above discussion we can find that the complexity of the optimal algorithm is high when the cooperative mode is involved, especially when the number of users is large.

In Procedure 1, we calculate the EE values with three modes for relay-aided D2D pairs in all candidate cellular channels, a total of  $3M^2$  times at most. But for one relay-aided D2D pair, the mode with largest EE values in all channels may remain same. That means we can use the mode selection result on one random channel as the final result. Therefore, we can modify the step 2) of Procedure 1 as follows:

- For each D2D pair without relays in all candidate cellular channels, obtain the optimal power and EE values in direct mode, and select the EE as  $\eta_{ij}$ . For each D2D pair with relays in one random cellular channel, obtain the optimal power and EE values of three transmission modes, compare the EE values and select the largest one as  $\eta_{ij}$ . For the other channels, use the result of mode selection on the random channel as the final result, and obtain the EE values as  $\eta_{ij}$ .

The proposed low-complexity sub-optimal resource allocation scheme, i.e., Procedure 2, is summarized as in Figure 4. Compared to Procedure 1, the average time complexity of Procedure 2 decreases from  $\mathcal{O}(2M^2 W_1 W_2 + M^3)$  to  $\mathcal{O}(\frac{2}{3}M^2 W_1 W_2 + M^3)$ .

## VI. SIMULATION RESULTS

In this section, simulation results are presented to evaluate the performance of the proposed procedures and prove the effectiveness of the 3-D resource management scheme. Initially, we research the factors which influence the results of mode selection for one D2D pair. Then the system simulation for multiple D2D pairs is presented.

The simulation parameters are illustrated in Table 2. The circuit power of transmitting data and receiving data is the same to all UEs, denoted by  $P_0$ . In the following, the proposed algorithms are evaluated by Monte Carlo simulations. At each simulation trial, the CUEs, the D2D pairs, and the idle CUEs serve as candidate relays are randomly dropped. We focus on the scenario that relay selection has been done, and the large

TABLE 2. Simulation parameters.

Parameter	Value
$M$	10
$N$	4
Spectrum bandwidth	10 MHz
Noise PSD	-174 dBm/Hz
D2D pathloss	$148.1+40\lg[d(\text{km})]$ [46]
Cellular pathloss	$128.1+37.6\lg[d(\text{km})]$ [46]
$m_1$	1
$m_2$	2
$P_{\max}$	23 dBm
$\Upsilon_{\text{th}}^D$	0.5 bps/Hz
$\Upsilon_{\text{th}}^C$	0.5 bps/Hz
$P_0$	50 mW
Permissible error ( $\epsilon$ )	$10^{-3}$

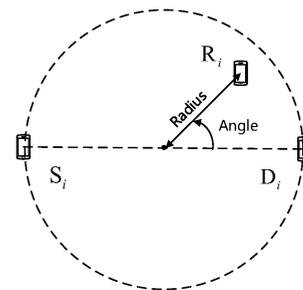


FIGURE 5. The location of relay.

number of idle CUEs ensures that each D2D pair has one relay. As shown in Figure 5,  $R_i$  may be located at any point in the circle whose center is the midpoint of the straight line between  $S_i$  and  $D_i$ . The location is described by radius and angle. To be specific, the radius denotes the distance from  $R_i$  to the midpoint, and the angle is in the range of  $[0, 2\pi)$ . BS is at the center of the cell and the uplink cellular signals without the co-channel interference are received at BS with the same SNR, i.e. 15 dB.

In following simulations, the proposed 3-D resource allocation algorithm is compared with three categories of existing works to reveal the contributions of this paper.

- *SE-max* algorithm in [17]: The transmit power is optimized to maximize SE under the constraints (26) and (27).
- 2-D resource allocation scheme, where only two dimensions of resource are optimized to maximize the EE of D2D communications, including *power-mode* scheme [26]–[28] and *mode-channel* scheme [29].
- Direct & two-hop scheme in [31]–[33] : 3-D resource allocation algorithm for D2D communications without cooperative mode.

### A. SIMULATION FOR ONE D2D PAIR

Figure 6 performs  $\eta_{ij}$  in direct mode of Dinkelbach algorithm and *SE-max* algorithm versus the distance of D2D,

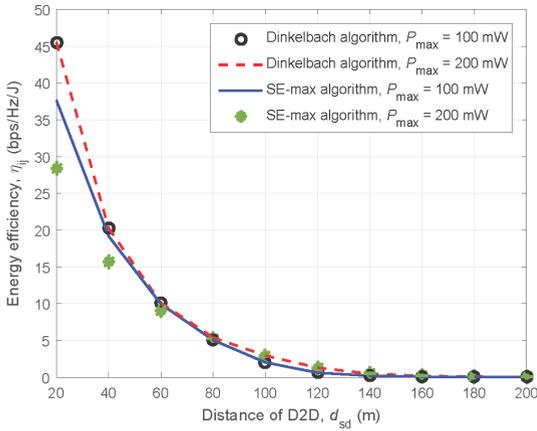


FIGURE 6. EE in direct mode versus  $d_{sd}$  with different  $P_{max}$  and different algorithms.

denoted by  $d_{sd}$ , with  $P_{max} = 100 mW$  and  $P_{max} = 200 mW$ . For a given  $P_{max}$ , Dinkelbach algorithm has higher  $\eta_{ij}$  than SE-max algorithm. Besides, in short range,  $\eta_{ij}$  of Dinkelbach algorithm with  $P_{max} = 100 mW$  and  $P_{max} = 200 mW$  are the same, which proves the optimal power value is less than  $100 mW$ . When  $d_{sd}$  is more than  $60 m$ ,  $\eta_{ij}$  with  $P_{max} = 200 mW$  is higher due to the change of the optimal power value. In long range,  $\eta_{ij}$  approaches zero.

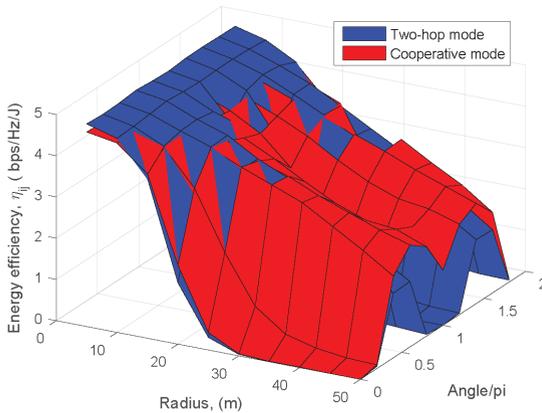


FIGURE 7. EE in two-hop mode and cooperative mode with AM algorithm versus the location of relay ( $d_{sd} = 100 m$ ).

As shown in Figure 7, we compare  $\eta_{ij}$  in two-hop mode and cooperative mode with AM algorithm versus the relay location when  $d_{sd}$  is  $100 m$ .  $\eta_{ij}$  reaches the top when  $R_i$  is near the midpoint, and decreases when far away. Meanwhile,  $\eta_{ij}$  in two-hop mode is higher than that in cooperative mode when the radius is small, and the situation is opposite when radius is more than  $20 m$ , indicating that the results of mode selection change. It is noticed that in cooperative mode  $\eta_{ij}$  drops slower with the relay moving because we exploit the  $S_i \rightarrow D_i$  communication link.

Figure 8 compares  $\eta_{ij}$  in three transmission modes versus  $d_{sd}$ . We observe that  $\eta_{ij}$  decreases with  $d_{sd}$  increasing. In direct mode,  $\eta_{ij}$  in  $20 m$  is  $35 bps/Hz/J$  higher than  $\eta_{ij}$

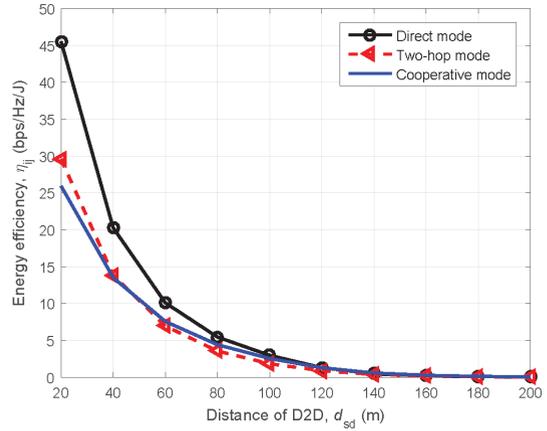


FIGURE 8. EE in three modes versus  $d_{sd}$ .

in  $60 m$ . The gap is  $23 bps/Hz/J$  in two-hop mode and  $18 bps/Hz/J$  in cooperative mode. Besides, in short range and medium range,  $\eta_{ij}$  in direct mode is the highest because the direct link is reliable and the power consumption of the relay can be saved. In long range,  $\eta_{ij}$  in cooperative mode is the highest due to the cooperation diversity at the destination. Therefore, it's necessary to select mode according to the link quality.

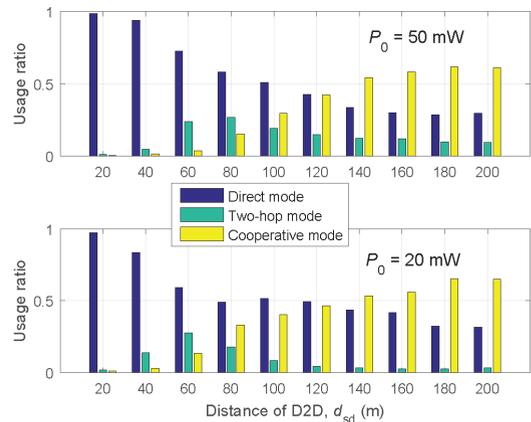


FIGURE 9. Usage ratio of three modes versus  $d_{sd}$  with different  $P_0$ .

To illustrate the specific influences of  $d_{sd}$  on the results of mode selection, the usage ratio versus  $d_{sd}$  with different  $P_0$  is plotted in Figure 9. Usage ratio refers to the ratio of total times when the specific mode is selected to the simulation times. As observed, the results of mode selection vary with  $d_{sd}$ , and the mode, which achieves the highest  $\eta_{ij}$  in Figure 8, is more likely to be selected. Two-hop mode has a lower ratio than the others because it suffers more negative influences from the random location of relays. It also shows differences between  $P_0 = 50 mW$  and  $P_0 = 20 mW$ . The superiority of cooperative mode is more obvious if  $P_0$  is smaller.

Figure 10 shows the effects of thresholds  $\Upsilon_{th}^D$  and  $\Upsilon_{th}^C$  on  $\eta_{ij}$  with different mode selection schemes. The thresholds

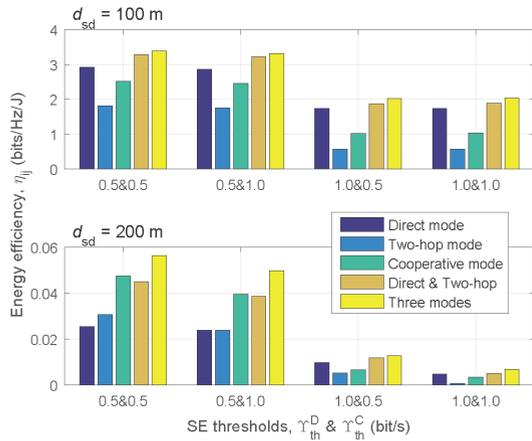


FIGURE 10. EE versus  $\gamma_{th}^D$  and  $\gamma_{th}^C$  with different mode selection schemes ( $m_2 = 1$ ).

guarantee the quality of service but limit the transmit power of D2D.  $\gamma_{th}^D$  determines the minimum required transmit power while  $\gamma_{th}^C$  bounds the maximal power. When  $d_{sd}$  remains unchanged, higher  $\gamma_{th}^D$  causes lower  $\eta_{ij}$ , and higher  $\gamma_{th}^C$  also brings loss. This situation is more noticeable when  $d_{sd}$  is larger. Besides, the mode selection scheme focusing direct mode and two-hop mode obtains lower EE than the mode selection scheme with three transmission mode, demonstrating the benefits of introducing cooperative mode. In some special case, such as  $d_{sd} = 200$  m,  $\gamma_{th}^D = 0.5$  bit/s, and  $\gamma_{th}^C = 0.5$  bit/s, the mode selection scheme only involves cooperative mode outperforms the mode selection scheme focusing direct mode and two-hop mode.

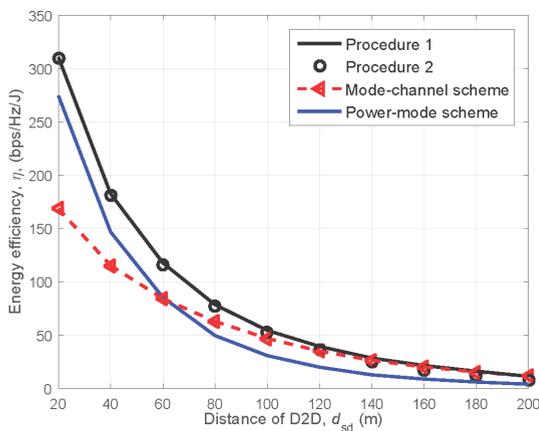


FIGURE 11. EE of Procedure 1, Procedure 2, and the 2-D schemes versus  $d_{sd}$ .

**B. SIMULATION FOR THE SYSTEM**

Figure 11 compares  $\eta$  of Procedure 1, Procedure 2 and the 2-D schemes versus  $d_{sd}$ . Procedure 1 achieves higher  $\eta$  than the 2-D schemes. But the gap between Procedure 1 and the mode-channel scheme is not obvious in long range. Meanwhile, compared with the power-mode scheme, the mode-channel scheme has a more serious degradation on the system

performance in short range. We can draw a conclusion that power allocation performs outstanding in short range and poor in long range, and channel assignment always performs well. Besides, it can be observed that Procedure 2 approximates Procedure 1 better in short range. The reason is that as  $d_{sd}$  increases,  $\eta$  suffers more influences from the difference in the results of mode selection when one D2D pair reuses different channels.

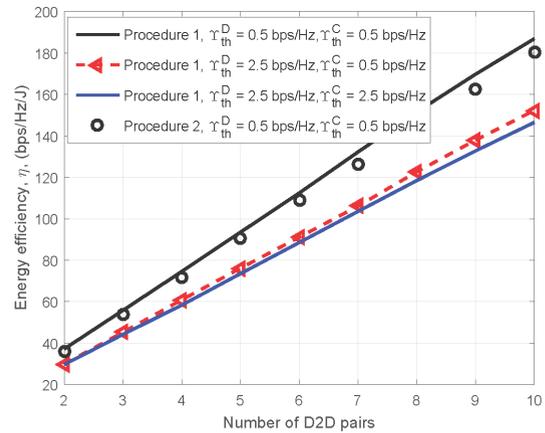


FIGURE 12. EE versus the number of D2D pairs with different  $\gamma_{th}^D$  and  $\gamma_{th}^C$  ( $m_2 = 1, d_{sd} \in [20m, 200m]$ ).

Figure 12 depicts  $\eta$  versus the number of D2D pairs with different  $\gamma_{th}^D$  and  $\gamma_{th}^C$ . Different from Figure 10, each D2D pair has a random  $d_{sd}$ , leading to more complicated resource management according to the previous analysis and simulations. It can be observed that  $\eta$  increases with the number of D2D pairs, while drops with higher  $\gamma_{th}^D$  and  $\gamma_{th}^C$ . For the system of D2D communications, higher received thresholds cause that the transmit power is far away from the optimal point and  $\eta$  decreases. Besides, the simulation results show that  $\eta$  by Procedure 2 reaches about 96.2% of  $\eta$  by Procedure 1 on average.

**VII. CONCLUSION**

In this paper, we have discussed the joint power allocation, mode selection and channel assignment for underlaid D2D communications in a multi-user scenario. The 3-D power-mode-channel problem has been decoupled into several steps without loss of optimality. Based on the optimal algorithm, a sub-optimal algorithm has been proposed to lower the complexity. Specifically, we have given the procedure of the proposed algorithms, and derived the average time complexity to prove the improvement. Simulation results have been provided to verify that the result of mode selection is affected by various factors, such as D2D distance, the location of relay, the circuit power and the QoS. Last but not least, the 3-D algorithm has better performance than 2-D algorithms, supporting the low-carbon wireless communications in 5G.

## APPENDIX

Here, taking power allocation for D2D communications in direct mode as an example, we present the detailed process of employing Dinkelbach Algorithm to obtain optimal transmit power.

---

### Algorithm 2 Dinkelbach Algorithm

---

1: **Initialization:**

$j = 0$ ,  $\eta^{(0)} = 10^{-4}$ , permissible error  $\varepsilon = 10^{-3}$ .

2: **Iteration begins:**

3: Solve the following optimization problem to obtain the transmit power  $P_s^{*(j)}$ :

$$\text{maximize}_{\left\{P_s^{(j)}\right\} \in \Omega} \left\{ R_d^1 \left( P_s^{(j)} \right) - \eta^{(j)} \left( \lambda P_s^{(j)} + P_{\text{cps}}^1 \right) \right\}.$$

4: Set  $f \left( \eta^{(j)} \right) = R_d^1 \left( P_s^{*(j)} \right) - \eta^{(j)} \left( \lambda P_s^{*(j)} + P_{\text{cps}}^1 \right)$ .

5: If  $|f \left( \eta^{(j)} \right)| \geq \varepsilon$ , update  $\eta^{(j)} = \frac{R_d^1 \left( P_s^{*(j)} \right)}{\lambda P_s^{*(j)} + P_{\text{cps}}^1}$ ,  $j = j + 1$ ,

return 3, otherwise continue.

6: **Iteration ends**

7: Output  $P_s^{*(j)}$ ,  $\eta^* = \eta^{(j)}$ .

---

## REFERENCES

- [1] G. Han, L. Wan, J. J. P. C. Rodrigues, H. Wu, and D. Zhang, "IEEE access special section editorial: Green communications and networking for 5G," *IEEE Access*, vol. 6, pp. 79263–79271, 2018.
- [2] G. Fodor et al., "An overview of device-to-device communications technology components in METIS," *IEEE Access*, vol. 4, pp. 3288–3299, 2016.
- [3] Z. Huang, H. Tian, S. Fan, Z. Xing, and X. Zhang, "Social-aware resource allocation for content dissemination networks: An evolutionary game approach," *IEEE Access*, vol. 5, pp. 9568–9579, 2017.
- [4] M. Nitti, V. Popescu, and M. Fadda, "Using an IoT platform for trustworthy D2D communications in a real indoor environment," *IEEE Trans. Netw. Service Manage.*, to be published.
- [5] R. Zhang, Y. Li, C.-X. Wang, Y. Ruan, Y. Fu, and H. Zhang, "Energy-spectral efficiency trade-off in underlying mobile D2D communications: An economic efficiency perspective," *IEEE Trans. Wireless Commun.*, vol. 17, no. 7, pp. 4288–4301, Jul. 2018.
- [6] N. Vo, T. Q. Duong, M. Guizani, and A. Kortun, "5G optimized caching and downlink resource sharing for smart cities," *IEEE Access*, vol. 6, pp. 31457–31468, 2018.
- [7] C.-X. Wang, J. Bian, J. Sun, W. Zhang, and M. Zhang, "A survey of 5G channel measurements and models," *IEEE Commun. Surveys Tuts.*, vol. 20, no. 4, pp. 3142–3168, 4th Quart., 2018.
- [8] X. Cheng, L. Yang, and X. Shen, "D2D for intelligent transportation systems: A feasibility study," *IEEE Trans. Intell. Trans. Syst.*, vol. 16, no. 4, pp. 1784–1793, Jan. 2015.
- [9] F. Jameel, Z. Hamid, F. Jabeen, S. Zeedally, and M. A. Javed, "A survey of device-to-device communications: Research issues and challenges," *IEEE Commun. Surveys Tuts.*, vol. 20, no. 3, pp. 2133–2168, 3rd Quart., 2018.
- [10] Y. Zhao et al., "Social-aware resource allocation for device-to-device communications underlying cellular networks," *IEEE Trans. Wireless Commun.*, vol. 14, no. 12, pp. 6621–6634, Dec. 2015.
- [11] R. Zhang, Y. Li, C.-X. Wang, Y. Ruan, and H. Zhang, "Energy efficiency of relay aided D2D communications underlying cellular networks," in *Proc. IEEE PIMRC*, Montreal, QC, Canada, Oct. 2017, pp. 1–5.
- [12] R. Atat, L. Liu, J. Ashdown, M. Medley, and J. Matyjas, "On the performance of relay-assisted D2D networks under spatially correlated interference," in *Proc. IEEE GLOBECOM*, Washington, DC, USA, Dec. 2016, pp. 1–6.
- [13] L. Jiang et al., "Social-aware energy harvesting device-to-device communications in 5G networks," *IEEE Wireless Commun.*, vol. 23, no. 4, pp. 20–27, Aug. 2016.
- [14] M. Nitti, G. A. Stelea, V. Popescu, and M. Fadda, "When social networks meet D2D communications: A survey," *Sensors*, vol. 19, no. 2, pp. 396–412, Jan. 2019.
- [15] R. Zhang, Y. Li, C.-X. Wang, Y. Ruan, and H. Zhang, "Performance tradeoff in relay aided D2D-cellular networks," *IEEE Trans. Veh. Technol.*, vol. 67, no. 10, pp. 10144–10149, Oct. 2018.
- [16] N. Lee, X. Lin, J. G. Andrews, and R. W. Heath, Jr., "Power control for D2D underlaid cellular networks: Modeling, algorithms, and analysis," *IEEE J. Sel. Areas Commun.*, vol. 33, no. 1, pp. 1–13, Jan. 2015.
- [17] X. Liu, Q. He, Y. Li, and J. Wang, "Large-scale fading based power allocation for Device-to-Device underlay cellular communication," in *Proc. IEEE VTC-Spring*, Glasgow, U.K., May 2015, pp. 1–5.
- [18] R. Wang, J. Liu, G. P. Zhang, S. H. Huang, and M. Yuan, "Energy efficient power allocation for relay-aided D2D communications in 5G networks," *China Commun.*, vol. 14, no. 6, pp. 54–64, 2017.
- [19] F. Hussain, M. Y. Hassan, M. S. Hossen, and S. Choudhury, "System capacity maximization with efficient resource allocation algorithms in D2D communication," *IEEE Access*, vol. 6, pp. 32409–32424, 2018.
- [20] L. Ren, M. Zhao, X. Gu, and L. Zhang, "A two-step resource allocation algorithm for D2D communication in full duplex cellular network," in *Proc. IEEE PIMRC*, Valencia, Spain, Sep. 2016, pp. 1–7.
- [21] H. Xu, W. Xu, Z. Yang, Y. Pan, J. Shi, and M. Chen, "Energy-efficient resource allocation in D2D underlaid cellular uplinks," *IEEE Commun. Lett.*, vol. 21, no. 3, pp. 560–563, Mar. 2017.
- [22] Y. Jiang, Q. Liu, F. Zheng, X. Gao, and X. You, "Energy-efficient joint resource allocation and power control for D2D communications," *IEEE Trans. Veh. Technol.*, vol. 65, no. 8, pp. 6119–6127, Aug. 2016.
- [23] Z. Zhou, G. Ma, D. Zhang, and C. Xu, "Energy-efficient context-aware resource allocation in D2D communications: An iterative matching approach," in *Proc. ICTC*, Jeju, South Korea, Oct. 2016, pp. 90–96.
- [24] Z. Zhou, K. Ota, M. Dong, and C. Xu, "Energy-efficient matching for resource allocation in D2D enabled cellular networks," *IEEE Trans. Veh. Technol.*, vol. 66, no. 6, pp. 5256–5268, Jun. 2017.
- [25] Z. Zhou, M. Dong, K. Ota, G. Wang, and L. T. Yang, "Energy-efficient resource allocation for D2D communications underlying cloud-RAN-based LTE-A networks," *IEEE Trans. Veh. Technol.*, vol. 3, no. 3, pp. 428–438, Jun. 2016.
- [26] K. S. Ali, H. ElSawy, and M.-S. Alouini, "On mode selection and power control for uplink D2D communication in cellular networks," in *Proc. IEEE Int. Conf. Commun. Workshops (ICC)*, Jun. 2015, pp. 620–626.
- [27] H. Gao, M. Wang, and T. Lv, "Energy efficiency and spectrum efficiency tradeoff in the D2D-enabled HetNet," *IEEE Trans. Veh. Technol.*, vol. 66, no. 11, pp. 10583–10587, Nov. 2017.
- [28] B. Ma, H. Zhang, and Z. Zhang, "Joint power allocation and mode selection for D2D communications with imperfect CSI," *China Commun.*, vol. 12, no. 7, pp. 73–81, Jul. 2015.
- [29] Y. Li, M. C. Gursoy, and S. Velipasalar, "Joint mode selection and resource allocation for D2D communications under queueing constraints," in *Proc. IEEE INFOCOM WKSHPS*, San Francisco, CA, USA, Apr. 2016, pp. 490–495.
- [30] D. Wu, J. Wang, R. Q. Hu, Y. Cai, and L. Zhou, "Energy-efficient resource sharing for mobile device-to-device multimedia communications," *IEEE Trans. Veh. Technol.*, vol. 63, no. 5, pp. 2093–2103, Jun. 2014.
- [31] S. Guo, X. Zhou, S. Xiao, and M. Sun, "Fairness-aware energy-efficient resource allocation in D2D communication networks," *IEEE Syst. J.*, to be published.
- [32] T. D. Hoang, L. B. Le, and T. Le-Ngoc, "Joint mode selection and resource allocation for relay-based D2D communications," *IEEE Commun. Lett.*, vol. 21, no. 2, pp. 398–401, Feb. 2017.
- [33] R. Ma, N. Xia, H.-H. Chen, C.-Y. Chiu, and C.-S. Yang, "Mode selection, radio resource allocation, and power coordination in D2D communications," *IEEE Wireless Commun.*, vol. 24, no. 3, pp. 112–121, Feb. 2017.
- [34] D. Feng et al., "Mode switching for energy-efficient device-to-device communications in cellular networks," *IEEE Trans. Wireless Commun.*, vol. 14, no. 12, pp. 6993–7003, Dec. 2015.
- [35] C. F. M. E. Silva, T. F. Maciel, R. L. Batista, L. Elias, A. Robson, and F. R. P. Cavalcanti, "Network-assisted neighbor discovery based on power vectors for D2D communications," in *Proc. IEEE VTC-Spring*, Glasgow, U.K., May 2015, pp. 1–5.
- [36] H. Tang, Z. Ding, and B. C. Levy, "D2D neighbor discovery and resource scheduling through demodulation reference signal," in *Proc. IEEE VTC-Fall*, Montreal, QC, Canada, Sep. 2016, pp. 1–6.
- [37] S. Wu, C.-X. Wang, H. Aggoune, M. M. Alwakeel, and X. You, "A general 3-D non-stationary 5G wireless channel model," *IEEE Trans. Commun.*, vol. 66, no. 7, pp. 3065–3078, Jul. 2018.

- [38] W. Cheng, X. Zhang, and H. Zhang, "QoS driven power allocation over full-duplex wireless links," in *Proc. IEEE ICC*, Ottawa, ON, Canada, Jun. 2012, pp. 5286–5290.
- [39] J. N. Laneman, D. N. C. Tse, and G. W. Wornell, "Cooperative diversity in wireless networks: Efficient protocols and outage behavior," *IEEE Trans. Inf. Theory*, vol. 50, no. 12, pp. 3062–3080, Dec. 2004.
- [40] W. Zhang, C.-X. Wang, D. Chen, and H. Xiong, "Energy-spectral efficiency tradeoff in cognitive radio networks," *IEEE Trans. Veh. Technol.*, vol. 65, no. 4, pp. 2208–2218, Apr. 2016.
- [41] T. D. Hoang, L. B. Le, and T. Le-Ngoc, "Energy-efficient resource allocation for D2D communications in cellular networks," *IEEE Trans. Veh. Technol.*, vol. 65, no. 9, pp. 6972–6986, Sep. 2016.
- [42] O. Amin, E. Beder, M. H. Ahmed, O. A. Dobre, and M. S. Alouini, "Opportunistic energy-aware amplify-and-forward cooperative systems with imperfect CSI," *IEEE Trans. Veh. Technol.*, vol. 65, no. 7, pp. 4875–4886, Jul. 2016.
- [43] W. Dinkelbach, "On nonlinear fractional programming," *Manage. Sci.*, vol. 13, no. 7, pp. 492–498, Mar. 1967.
- [44] B. Matthiesen, A. Zappone, and E. A. Jorswieck, "Resource allocation for energy-efficient 3-way relay channels," *IEEE Trans. Wireless Commun.*, vol. 14, no. 8, pp. 4454–4468, Aug. 2015.
- [45] S. Schaible, "Fractional programming. II, on Dinkelbach's algorithm," *Manage. Sci.*, vol. 22, no. 8, pp. 868–873, Apr. 1976.
- [46] Y. Dai, M. Sheng, K. Zhao, L. Liu, J. Liu, and J. Li, "Interference-aware resource allocation for D2D underlaid cellular network using SCMA: A hypergraph approach," in *Proc. IEEE WCNC*, Doha, Qatar, Apr. 2016, pp. 1–6.



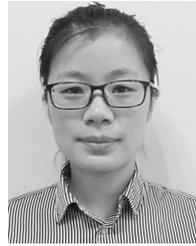
**RUI ZHANG** received the B.S., M.S., and Ph.D. degrees in telecommunications engineering from Xidian University, Xi'an, China, in 2012, 2015, and 2018, respectively. He was a Visiting Student with Heriot-Watt University, Edinburgh, U.K., from 2016 to 2017, under the supervision of Prof. C.-X. Wang. His current research interests include device-to-device communications, vehicle-to-vehicle communications, radio resource allocation techniques, and energy efficient wireless networks.



**CHUHAN QI** received the B.S. degree in telecommunications engineering from Xidian University, Xi'an, China, in 2012, where she is currently pursuing the M.S. degree in communication and information systems. Her current research interests include device-to-device communications, machine type communications, and radio resource allocation techniques.



**YONGZHAO LI** (M'04–SM'18) received the B.S., M.S., and Ph.D. degrees in electronic engineering from Xidian University, Xi'an, China, in 1996, 2001, and 2005, respectively. He was a Research Professor with the University of Delaware, Delaware, USA, from 2007 to 2008, and the University of Bristol, Bristol, U.K., in 2011, respectively. Since 1996, he has been with Xidian University, where he is currently a Full Professor with the State Key Laboratory of Integrated Services Networks. He has published more than 50 journal papers and 20 conference papers. His research interests include wideband wireless communications, signal processing for communications, and spatial communications networks. In 2008, he received the Best Paper Award of IEEE ChinaCOM'08 International Conference. Due to his excellent contributions in education and research, in 2012, he received the Program for New Century Excellent Talents in University, Ministry of Education, China. He currently serves as the Vice Dean of Graduate School, Xidian University.



**YUHAN RUAN** received the B.S. and Ph.D. degrees in telecommunications engineering from Xidian University, Xi'an, China, in 2013 and 2018, respectively. She was a Visiting Ph.D. Student with Heriot-Watt University, Edinburgh, U.K., from 2016 to 2017, under the supervision of Prof. C.-X. Wang. Her current research interests include satellite-terrestrial networks, cooperative communications, cognitive radio techniques, and energy efficient wireless networks.



**CHENG-XIANG WANG** (S'01–M'05–SM'08–F'17) received the B.Sc. and M.Eng. degrees in communication and information systems from Shandong University, China, in 1997 and 2000, respectively, and the Ph.D. degree in wireless communications from Aalborg University, Denmark, in 2004.

He was a Research Assistant with the Hamburg University of Technology, Hamburg, Germany, from 2000 to 2001, a Research Fellow with the University of Agder, Grimstad, Norway, from 2001 to 2005, and a Visiting Researcher with Siemens AG Mobile Phones, Munich, Germany, in 2004. He has been with Heriot-Watt University, Edinburgh, U.K., since 2005, where he was promoted to a Professor, in 2011. In 2018, he joined Southeast University, China, as a Professor. He has authored three books, one book chapter, and more than 350 papers in refereed journals and conference proceedings, including 23 highly cited papers. He has also delivered 17 invited keynote speeches/talks and six tutorials in international conferences. His current research interests include wireless channel measurements and modeling, (B)5G wireless communication networks, and applying artificial intelligence to wireless communication networks.

Dr. Wang has served as a TPC Member of more than 80 international conferences. He is a Fellow of the IET, the IEEE Communications Society Distinguished Lecturer, in 2019 and 2020, and a Highly-Cited Researcher recognized by Clarivate Analytics, in 2017 and 2018. He has received nine Best Paper Awards from the IEEE GLOBECOM 2010, the IEEE ICCT 2011, ITST 2012, the IEEE VTC 2013-Spring, IWCMC 2015, IWCMC 2016, the IEEE/CIC ICC 2016, and WPMC 2016. He has served as the TPC Chair and the General Chair for more than 80 international conferences. He has served as an Editor for nine international journals, including the IEEE TRANSACTIONS ON WIRELESS COMMUNICATIONS, from 2007 to 2009, the IEEE TRANSACTIONS ON VEHICULAR TECHNOLOGY, from 2011 to 2017, and the IEEE TRANSACTIONS ON COMMUNICATIONS, from 2015 to 2017. He was a Guest Editor of the IEEE JOURNAL ON SELECTED AREAS IN COMMUNICATIONS, with the special issue on Vehicular Communications and Networks (Lead Guest Editor), the special issue on Spectrum and Energy Efficient Design of Wireless Communication Networks, and the special issue on Airborne Communication Networks. He was also the Guest Editor of the IEEE TRANSACTIONS ON BIG DATA with the special issue on Wireless Big Data.



**HAILIN ZHANG** (M'98) received the B.S. and M.S. degrees from Northwestern Polytechnic University, Xi'an, China, in 1985 and 1988, respectively, and the Ph.D. degree from Xidian University, Xi'an, China, in 1991, where he has been, since 1991 and he is currently a Senior Professor and a Ph.D. Adviser with the School of Telecommunications Engineering. He is also the Director of the Key Laboratory in Wireless Communications Sponsored by the China Ministry of Information Technology, a Key Member of the State Key Laboratory of Integrated Services Networks, one of the State Government Specially Compensated Scientists and Engineers, a Field Leader in telecommunications and information systems with Xidian University, and the Associate Director for National 111 Project. He has recently published 78 papers in telecommunications journals and proceedings. His current research interests include key transmission technologies and standards on broadband wireless communications for 4G, 5G, and next generation broadband wireless access systems.